Digital Signal Processing Assignment # 6

1. Find the DTFT of the following signals.

(a)
$$x(n) = a^n [u(n) - u(n - n_0)]$$

(b)
$$x(n) = n \left(\frac{1}{3}\right)^{|n|}$$

(c)
$$x(n) = a^n \cos(\Omega_0 n) u(n), |a| < 1$$

(d)
$$x(n) = (n-1)a^n u(n), |a| < 1$$

2. Find x(n) with DTFT in $0 \le \Omega \le 2\pi$ given as follows

(a)
$$X(\Omega) = -j\pi\delta\left(\Omega - \frac{\pi}{3}\right) + \pi\delta\left(\Omega - \frac{2\pi}{3}\right)$$

(b)
$$X(\Omega) = \frac{4}{[\exp(-j\Omega) - 2]^2}$$

3. Find the frequency response of the system described by the following difference equation, and plot the amplitude and phase response with Matlab.

$$y(n) - 0.5y(n-2) = 2x(n) - x(n-1) - 0.5x(n-2)$$
 (1)