

ELEG 3124 Assignment # 12

1. The Laplace transform of a causal signal $x(t)$ is

$$X(s) = \frac{s + 5}{s^2 + 3s + 2}, \quad \text{Re}(s) > -1 \quad (1)$$

Using the properties of Laplace transform, find the Laplace transform of the following signals

- (a) $3x(t/3)$
 - (b) $x(t - 2)$
 - (c) $(t - 1)x(t)$.
 - (d) $\frac{dx(t)}{dt}$.
 - (e) $x(t) \exp(-2t)$.
 - (f) $x(t) \cos(2t)$ (don't need to simplify)
2. Determine the initial value and final value of the signal whose Laplace transform is $X(s) = \frac{s+2}{s^2-2s-3}$.
3. Solve the following differential equation:

$$y''(t) + 4y'(t) + 3y(t) = \exp(-2t)u(t), \quad y(0^-) = 0, \quad y'(0^-) = 1 \quad (2)$$